Welcome to Michigan’s K-8 Grade Level Content Expectations

Purpose & Overview

In 2004, the Michigan Department of Education embraced the challenge of creating Grade Level Content Expectations in response to the federal No Child Left Behind Act of 2001. This act mandated the existence of a set of comprehensive state grade level assessments that are designed based on rigorous grade level content.

In this global economy, it is essential that Michigan students possess personal, social, occupational, civic, and quantitative literacy. Mastery of the knowledge and essential skills defined in Michigan’s Grade Level Content Expectations will increase students’ ability to be successful academically, contribute to the future businesses that employ them and the communities in which they choose to live.

The Grade Level Content Expectations build from the Michigan Curriculum Framework and its Teaching and Assessment Standards. Reflecting best practices and current research, they provide a set of clear and rigorous expectations for all students and provide teachers with clearly defined statements of what students should know and be able to do as they progress through school.

Why Create a 12.05 Version of the Expectations?

The Office of School Improvement is committed to creating the best possible product for educators. This commitment served as the impetus for the revision of the 6.04 edition that was previously released in June of 2004. This new version, v.12.05, refines and clarifies the original expectations, while preserving their essence and original intent.

As education continues to evolve, it is important to remember that each curriculum document should be considered as a work in progress, and will continue to be refined to improve the quality.

The revision process greatly improved the continuity from one grade to the next, and better ensured coherence both in content and pedagogy. To obtain more specific details about the revisions, please refer to the addendum included in this document. The forward of the Across the Grades v.12.05 companion document also clarifies the types of changes made. Educators can access the Across the Grades companion document by visiting the Michigan Department of Education Grade Level Content Expectations web page at www.michigan.gov/glce.

Assessment

The Grade Level Content Expectations document is intended to be a state assessment tool with the expectations written to convey expected performances by students. The Office of Assessment and Accountability was involved in the development of version 12.05 and has incorporated the changes in the construction of test and item specifications for the K-8 Michigan Education Assessment Program (MEAP) and MI-Access. This updated version will assist us in the creation of companion documents, content examples, and to guide program planners in focusing resources and energy.
Curriculum
Using this document as a focal point in the school improvement process, schools and districts can generate conversations among stakeholders concerning current policies and practices to consider ways to improve and enhance student achievement. Together, stakeholders can use these expectations to guide curricular and instructional decisions, identify professional development needs, and assess student achievement.

Understanding the Organizational Structure
The expectations in this document are divided into strands with multiple domains within each, as shown below. The skills and content addressed in these expectations will in practice be woven together into a coherent, Mathematics curriculum. The domains in each mathematics strand are broader, more conceptual groupings. In several of the strands, the “domains” are similar to the “standards” in Principles and Standards for School Mathematics from the National Council of Teachers of Mathematics.

To allow for ease in referencing expectations, each expectation has been coded with a strand, domain, grade-level, and expectation number. For example, M.UN.00.01 indicates:

- M - Measurement strand
- UN - Units & systems of measurement domain of the Measurement strand
- 00 - Kindergarten Expectation
- 01 - First Expectation in the Grade-Level view of the Measurement strand

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<th>Strand 5 Data and Probability</th>
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<td>Meaning, notation, place value, and comparisons (ME)</td>
<td>Patterns, relations, functions, and change (PA)</td>
<td>Units and systems of measurement (UN)</td>
<td>Geometric shape, properties, and mathematical arguments (GS)</td>
<td>Data representation (RE)</td>
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<tr>
<td>Number relationships and meaning of operations (MR)</td>
<td>Representation (RP)</td>
<td>Techniques and formulas for measurement (TE)</td>
<td>Location and spatial relationships (LO)</td>
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<td>Fluency with operations and estimation (FL)</td>
<td>Formulas, expressions, equations, and inequalities (RP)</td>
<td>Problem solving involving measurement (PS)</td>
<td>Spatial reasoning and geometric modeling (SR)</td>
<td>Probability (PR)</td>
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Preparing Students for Academic Success
Within the hands of teachers, the Grade Level Content Expectations are converted into exciting and engaging learning for Michigan’s students. As we use these expectations to develop units of instruction and plan instructional delivery, it is critical to keep in mind that content knowledge alone is not sufficient for academic success. Students must be able to apply knowledge in new situations, to solve problems by generating new ideas, and to make connections between what they learn in class to the world around them. The art of teaching is what makes the content of learning become a reality.

Through the collaborative efforts of Michigan educators and creation of professional learning communities, we can enable our young people to attain the highest standards, and thereby open doors for them to have fulfilling and successful lives.
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<th>NUMBER AND OPERATIONS</th>
<th>Understand derived quantities</th>
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<td><strong>N.MR.07.02</strong> Solve problems involving derived quantities such as density, velocity, and weighted averages.*</td>
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<table>
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<tr>
<th>Understand and solve problems involving rates, ratios, and proportions</th>
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<tr>
<td><strong>N.FL.07.03</strong> Calculate rates of change including speed.</td>
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<tr>
<td><strong>N.MR.07.04</strong> Convert ratio quantities between different systems of units, such as feet per second to miles per hour.</td>
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<tr>
<td><strong>N.FL.07.05</strong> Solve proportion problems using such methods as unit rate, scaling, finding equivalent fractions, and solving the proportion equation ( \frac{a}{b} = \frac{c}{d} ); know how to see patterns about proportional situations in tables.*</td>
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<th>Recognize irrational numbers</th>
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<td><strong>N.MR.07.06</strong> Understand the concept of square root and cube root, and estimate using calculators.</td>
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<th>Compute with rational numbers</th>
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<td><strong>N.FL.07.07</strong> Solve problems involving operations with integers.</td>
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<td><strong>N.FL.07.08</strong> Add, subtract, multiply, and divide positive and negative rational numbers fluently.*</td>
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<tr>
<td><strong>N.FL.07.09</strong> Estimate results of computations with rational numbers.</td>
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* revised expectations in italics
ALGEBRA

Understand and apply directly proportional relationships and relate to linear relationships

A.PA.07.01 Recognize when information given in a table, graph, or formula suggests a directly proportional or linear relationship.*

A.RP.07.02 Represent directly proportional and linear relationships using verbal descriptions, tables, graphs, and formulas, and translate among these representations.

A.PA.07.03 Given a directly proportional or other linear situation, graph and interpret the slope and intercept(s) in terms of the original situation; evaluate \( y = mx + b \) for specific \( x \) values, e.g., weight vs. volume of water; base cost plus cost per unit.*

A.PA.07.04 For directly proportional or linear situations, solve applied problems using graphs and equations, e.g., the heights and volume of a container with uniform cross-section; height of water in a tank being filled at a constant rate; degrees Celsius and degrees Fahrenheit; distance and time under constant speed.

A.PA.07.05 Recognize and use directly proportional relationships of the form \( y = mx \), and distinguish from linear relationships of the form \( y = mx + b \), \( b \) non-zero; understand that in a directly proportional relationship between two quantities one quantity is a constant multiple of the other quantity.*

Understand and represent linear functions

A.PA.07.06 Calculate the slope from the graph of a linear function as the ratio of “rise/run” for a pair of points on the graph, and express the answer as a fraction and a decimal; understand that linear functions have slope that is a constant rate of change.

A.PA.07.07 Represent linear functions in the form \( y = x + b \), \( y = mx \), and \( y = mx + b \), and graph, interpreting slope and \( y \)-intercept.

A.FO.07.08 Find and interpret the \( x \) and/or \( y \) intercepts of a linear equation or function. Know that the solution to a linear equation of the form \( ax + b = 0 \) corresponds to the point at which the graph of \( y = ax + b \) crosses the \( x \) axis.*

Understand and solve problems about inversely proportional relationships

A.PA.07.09 Recognize inversely proportional relationships in contextual situations; know that quantities are inversely proportional if their product is constant, e.g., the length and width of a rectangle with fixed area, and that an inversely proportional relationship is of the form \( y = \frac{k}{x} \) where \( k \) is some non-zero number.

A.RP.07.10 Know that the graph of \( y = \frac{k}{x} \) is not a line, know its shape, and know that it crosses neither the \( x \) nor the \( y \)-axis.

Apply basic properties of real numbers in algebraic contexts

A.PA.07.11 Understand and use basic properties of real numbers: additive and multiplicative identities, additive and multiplicative inverses, commutativity, associativity, and the distributive property of multiplication over addition.

Combine algebraic expressions and solve equations

A.FO.07.12 Add, subtract, and multiply simple algebraic expressions of the first degree, e.g., \( (9x + 8y) - 5x + y \) or \( x(x+2) \) and justify using properties of real numbers.*

A.FO.07.13 From applied situations, generate and solve linear equations of the form \( ax + b = c \) and \( ax + b = cx + d \), and interpret solutions.*

* revised expectations in italics
### GEOMETRY
**Draw and construct geometric objects**

- **G.SR.07.01** Use a ruler and other tools to draw squares, rectangles, triangles, and parallelograms with specified dimensions.
- **G.SR.07.02** Use compass and straightedge to perform basic geometric constructions: the perpendicular bisector of a segment, an equilateral triangle, and the bisector of an angle; understand informal justifications.

**Understand the concept of similar polygons, and solve related problems**

- **G.TR.07.03** Understand that in similar polygons, corresponding angles are congruent and the ratios of corresponding sides are equal; understand the concepts of similar figures and scale factor.
- **G.TR.07.04** Solve problems about similar figures and scale drawings.
- **G.TR.07.05** Show that two triangles are similar using the criteria: corresponding angles are congruent (AAA similarity); the ratios of two pairs of corresponding sides are equal and the included angles are congruent (SAS similarity); ratios of all pairs of corresponding sides are equal (SSS similarity); use these criteria to solve problems and to justify arguments.
- **G.TR.07.06** Understand and use the fact that when two triangles are similar with scale factor of $r$, their areas are related by a factor of $r^2$. 

### DATA AND PROBABILITY

**Represent and interpret data**

- **D.RE.07.01** Represent and interpret data using circle graphs, stem and leaf plots, histograms, and box-and-whisker plots, and select appropriate representation to address specific questions.
- **D.AN.07.02** Create and interpret scatter plots and find line of best fit; use an estimated line of best fit to answer questions about the data.

**Compute statistics about data sets**

- **D.AN.07.03** Calculate and interpret relative frequencies and cumulative frequencies for given data sets.
- **D.AN.07.04** Find and interpret the median, quartiles, and interquartile range of a given set of data.